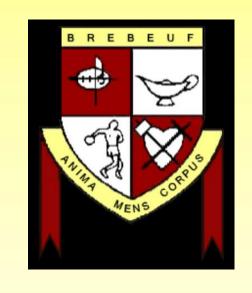
# ST. JEAN DE BREBEUF MATHEMATICS



# CHAPTER 1.5 MAKE DECISIONS

USING TRIGONOMETRY

### **KEY CONCEPTS**

Decide which formula or tool to use based on the type of triangle the situation presents.

If the problem is modelled by a <u>right triangle</u>, use the **primary trigonometric ratios**.

If the problem is modelled by an acute or obtuse triangle

→with two angles and a given side or two sides and an opposite angle, use the Sine Law

→with two sides and a contained angle (SAS) or three sides (SSS), use the Cosine Law

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BASIC TRIGONOMETRIC RATIOS	THE SINE LAW	THE COSINE LAW
$\sin A = \frac{OPPOSITE}{HYPOTENUSE}$ $\cos A = \frac{ADJACENT}{HYPOTENUSE}$	$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$	$a^{2} = b^{2} + c^{2} - 2bc \cos A$ $b^{2} = a^{2} + c^{2} - 2ac \cos B$ $c^{2} = a^{2} + b^{2} - 2ab \cos C$
$tan A = \frac{OPPOSITE}{ADJACENT}$	If the problem is modelled by an acute or obtuse triangle (non-right angled)	$\cos A = \frac{b^2 + c^2 - a^2}{2bc}$
If the problem is modelled by a <u>right</u> triangle, use the primary trigonometric ratios.	→with two angles and a given side or →two sides and an opposite angle, use the Sine Law	$\cos B = \frac{a^2 + c^2 - b^2}{2ac}$ $\cos C = \frac{a^2 + b^2 - c^2}{2ab}$

### PYTHAGOREAN THEOREM

$$c^2 = a^2 + b^2$$

**Pythagorean Theorem** is *only* used to solve for a missing side in a <u>right angle</u> triangle

If the problem is modelled by an acute or obtuse triangle (non right angle)
→ with two sides and a contained angle (SAS)

- → You use these formulas to solve for side length
- → Three sides (SSS), use the Cosine Law
- → You use these formulas to solve for angles

### THE COSINE LAW

$$a^{2} = b^{2} + c^{2} - 2bc \cos A$$
$$b^{2} = a^{2} + c^{2} - 2ac \cos B$$
$$c^{2} = a^{2} + b^{2} - 2ab \cos C$$

$$\cos A = \frac{b^2 + c^2 - a^2}{2bc}$$

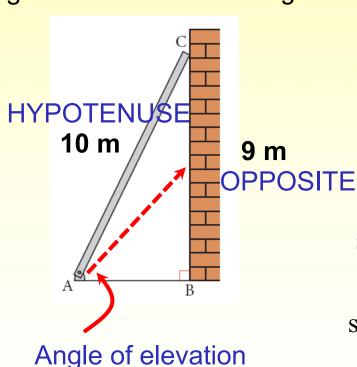
$$\cos B = \frac{a^2 + c^2 - b^2}{2ac}$$

$$\cos C = \frac{a^2 + b^2 - c^2}{2ab}$$



### **EXAMPLE 1**

A **10 m** ladder leans against a wall. The top of the ladder is **9 m** above the ground. What is the *angle of elevation* between the floor and the ladder?



**Inverse sin** 

sin

→ 2<sup>nd</sup>/Shift then

We have a **RIGHT TRIANGLE** 

→ Use basic trigonometric ratios

→ Label the *given* sides (with respect to the angle we are solving for) and determine which trigonometric ratio to use

$$\sin A = \frac{OPPOSITE}{HYPOTENUSE}$$

$$\sin A = \frac{9}{10}$$

$$\sin A = 0.9$$

$$\angle A = \sin^{-1}(0.9)$$

$$\angle A = 64^{\circ}$$

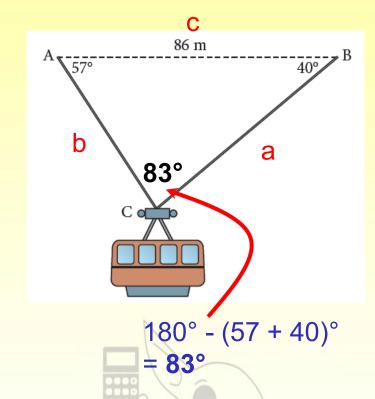
The angle of elevation between the floor and the ladder is **64**°.

FORMULAS

### **EXAMPLE 2**

A cable car stops part of the way across an **86** m wide gorge. The cable holding the car makes an *angle of depression* of **57**° at one end and an *angle of depression* of **40**° at the other end. How long is the cable that holds the car? Round your answer to the <u>nearest</u> metre.

Need to solve for "a" and "b" and add them together!



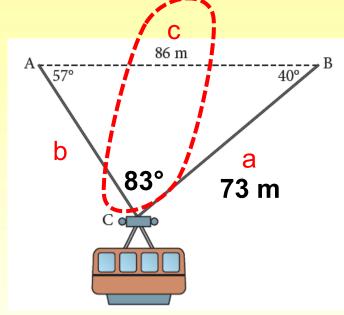
We are missing information

→ We can solve for the missing angle!



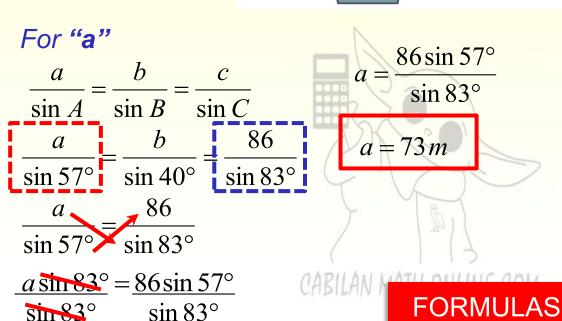
### **EXAMPLE 2**

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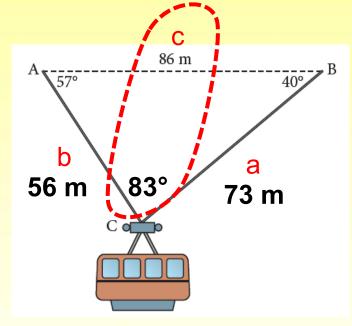
Need to solve for "a" and "b" and add them together!

We have an **angle** and a side *opposite* to the angle → Use **SINE LAW**!



### **EXAMPLE 2**

A cable car stops part of the way across an **86** m wide gorge. The cable holding the car makes an *angle of depression* of **57°** at one end and an *angle of depression* of **40°** at the other end. How long is the cable that holds the car? Round your answer to the <u>nearest</u> metre.



Need to solve for "a" and "b" and add them together!

→Use **SINE LAW!** 

The length of the cable that holds the car is **129 metres**.

For "b" (use given info for accuracy!)

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C} \qquad b = \frac{86 \sin 40^{\circ}}{\sin 83^{\circ}}$$

$$\frac{73}{\sin 57^{\circ}} = \frac{b}{\sin 40^{\circ}} = \frac{86}{\sin 83^{\circ}} \qquad b = 56m$$

$$\frac{b}{\sin 40^{\circ}} = \frac{86}{\sin 83^{\circ}} \qquad For length of cable$$

$$\frac{b \sin 83^{\circ}}{\sin 83^{\circ}} = \frac{86 \sin 40^{\circ}}{\sin 83^{\circ}} = \frac{73 m + 56 m}{\sin 83^{\circ}} = \frac{129 m}{\sin 83^{\circ}}$$

### **EXAMPLE 3**

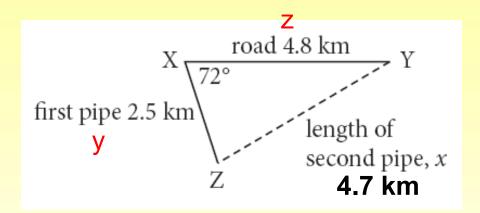
A sewer pipe for a new subdivision has to be laid underground. A connection is made to the main service pipe at either end of the 4.8 km stretch of road. One pipe, 2.5 km long, makes an angle of 72° at one end of the road.

(a) Calculate the length of the second pipe

We have an acute/non-right triangle

→side-angle-side (SAS)

→ Use COSINE LAW!



$$x^{2} = y^{2} + z^{2} - 2yz\cos X$$

$$x^{2} = (2.5)^{2} + (4.8)^{2} - 2(2.5)(4.8)(\cos 72^{\circ})$$

$$x^{2} = 21.8736$$

$$\sqrt{x^{2}} = \sqrt{21.8736}$$

$$x = 4.7$$

The length of the second pipe is **4.7 km** 



# CHAPTER 15 MAKE DEGISIONS USING TRIG

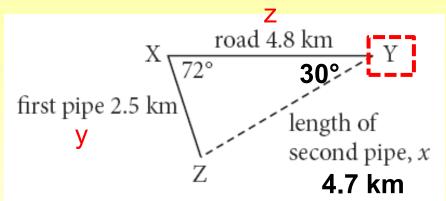
### **EXAMPLE 3**

A sewer pipe for a new subdivision has to be laid underground. A connection is made to the main service pipe at either end of the 4.8 km stretch of road. One pipe, 2.5 km long, makes an angle of 72° at one end of the road.

(b) Determine the angle **between the** second pipe and the road

Need to solve for  $\angle Y$ → Easiest to use SINE LAW!

> The angle between the second pipe and the road is 30°.



first pipe 2.5 km  

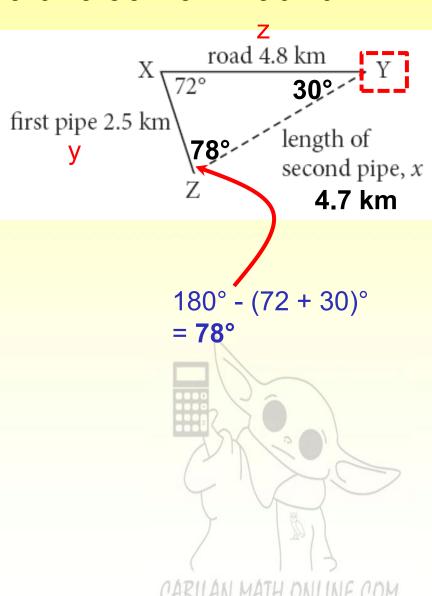
$$\frac{x}{\sin X} = \frac{y}{\sin Y} = \frac{z}{\sin Z}$$
  
 $\frac{4.7}{\sin 72^{\circ}} = \frac{2.5}{\sin Y} = \frac{4.8}{\sin Z}$  sin  $Y = 0.5059$   
 $\frac{4.7}{\sin 72^{\circ}} = \frac{2.5}{\sin Y}$   $2.5 = 2.5 =$ 

### **EXAMPLE 3**

A sewer pipe for a new subdivision has to be laid underground. A connection is made to the main service pipe at either end of the 4.8 km stretch of road. One pipe, 2.5 km long, makes an angle of 72° at one end of the road.

(c) What is the angle **between the first pipe and second pipe**?

The angle between the first and second pipe is **78**°.



# **Homework**

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### **BASIC TRIGONOMETRIC RATIOS**

$$\sin A = \frac{OPPOSITE}{HYPOTENUSE}$$

$$\cos A = \frac{ADJACENT}{HYPOTENUSE}$$

$$\tan A = \frac{OPPOSITE}{ADJACENT}$$

### SINE LAW

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

### **COSINE LAW**

$$a^{2} = b^{2} + c^{2} - 2bc \cos A$$

$$b^{2} = a^{2} + c^{2} - 2ac \cos B$$

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$$\cos A = \frac{b^2 + c^2 - a^2}{2bc}$$

$$\cos B = \frac{a^2 + c^2 - b^2}{2ac}$$

$$\cos C = \frac{a^2 + b^2 - c^2}{2ab}$$

**PREVIOUS** 

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